S.N. Bose National Centre for Basic Sciences Block-JD, Sector-3, Kolkata (700106)

INFINITY

Finite Attempts to Capture The Infinite

ANKUR SRIVASTAV (IPh-D 2nd year)

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"It is incumbent on the person who specializes in physics to discuss the infinite. And to inquire whether there is such a thing or not, and, if there is, what it is. "

Aristotle, Physics III, 202b34

Plan of Talk

CENTRE FOR BAGIC OCIENCES 1994-1974 1994-1974 1994-1974 1994-1974 1994-1974 1994-1974 1996-1996 1996-

Introduction

A Few Paradoxes

The Dichotomy (Zeno of Elea (c. 450 BC)) Galileo's Paradox Halley / Olber's Paradox

Infinity in Modern Physics

Infinite Divisibility of Space Infinite Extension of Space Dante's Universe

Conclusion

References and Bibliography





- The first recorded use of word "Infinite" is credited to Anaximander (pre-Socratic Greek philosopher).
- His term "apeiron" can be translated as limitless, boundless, indefinite, infinite.
- ► In 1655, the Oxford mathematician John Wallis ¹ first wrote down the 'lazy eight' symbol for Infinite - ∞

¹Famous for writing codes for both sides in the English Civil war.

Zeno of Elea





Figure: Zeno of Elea (c. 490-430 BC)

The Dichotomy



The Dichotomy paradox was put forward to show that motion is just an 'illusion'.



Figure: The Dichotomy

Because Zeno rejected the Infinite, he concluded that motion is not possible.

Galileo Galilei





Figure: Galileo Galilei (1564-1642)

Galileo's Paradox



- Put the set of integers in one-to-one correspondence with the set of square of integers.
- Galileo asked, which list is bigger?
- Because set of squares is already subset of set of integers, does infinity come in different sizes?
- Galileo never resolved this paradox. He only concluded -

"We cannot speak of infinite quantities as being the one greater or less than or equal to another."

Sir Edmund Halley





Figure: Sir Edmund Halley (1656-1736)

Halley / Olber's Paradox



- Another interesting paradox arises if one considers an infinite Universe.
- Sir Edmund Halley realized that a Universe containing infinite number of stars should shine like the surface of a star, day or night. But It Doesn't!



Figure: Looking into the woods. Everywhere your line of sight ends on a tree trunk.



- Two most powerful theories of 20th century are General Relativity and Quantum Theory.
- If we rely on these theories, taken together, we are forced to accept that space is not infinitely divisible. Space itself can be thought of as an ensemble of atoms of space.
- Notice that Zeno's Dichotomy paradox is resolved if space is not infinitely divisible.
- There is no necessarily infinite toward the small.²

Infinite Extension of Space Is Universe Infinite?



- Archytas of Tarentum was a 5th century Greek thinker.
- Archytas claimed that the Universe must be infinitely extended because of the following:

"If I arrived at the outermost edge of the heaven, could I extend my hand or staff into what is outside or not? It would be paradoxical not to be able to extend it."

Aristotle considered this argument to be "most important" reason why people believe in the existence of the infinite.

Dante Alighieri





Figure: Dante Alighieri (1265-1321)

Dante's Universe Finite Universe Without Boundary



- Middle Age poet, Dante, solved above problem by imagining geometry of Universe as a 3-sphere.
- This is precisely a geometry of Universe that emerges from Einstein's equations.³



Figure: Dante Alighieri (1265-1321)







We don't really know what infinity is, but there are strong reasons to believe that physical infinities are less likely.



References and Bibliography



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Thank you!